



Arts & Humanities
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voice and identity



Effects of the imbalance in the Log LR Cost Function (C_{llr})

Vincent Hughes

vincent.hughes@york.ac.uk

THE UNIVERSITY of York

1. Introduction

Essential elements of the *paradigm shift* across forensic science (Morrison 2014):

- (i) use of the **LR**
- (ii) testing **validity** (accuracy) & **reliability** (precision):
conducted using sets of SS and DS pairs where:
 - N SS pairs = N speakers
 - N DS pairs = min. (N speakers²)-N speakers

Validity metrics:

Equal Error Rate (EER):

- false hits (DS LLR>0) == misses (SS LLR<0)
- *accept-reject* decisions based on $p(H|E)$

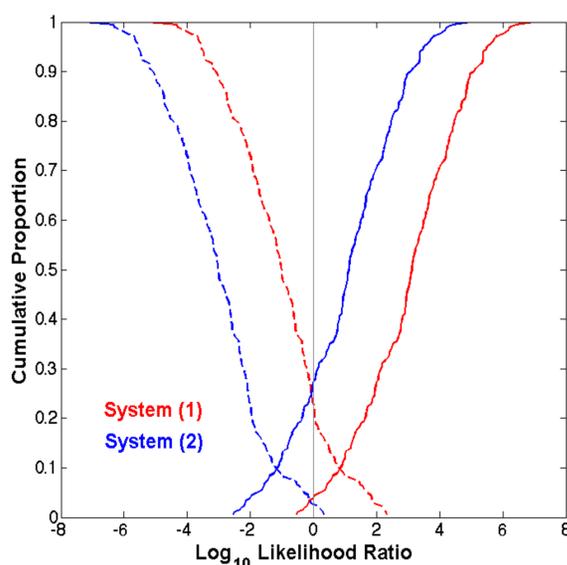
Log LR Cost Function (C_{llr}):

$$C_{llr} = \frac{1}{2} \left(\frac{1}{N_{ss}} \sum_{i=1}^{N_{ss}} \log_2 \left(1 + \frac{1}{LR_{ss_i}} \right) + \frac{1}{N_{ds}} \sum_{i=1}^{N_{ds}} \log_2 \left(1 + \frac{1}{LR_{ds_i}} \right) \right)$$

- based on magnitude of *contrary-to-fact* LLRs
- mean of two cost functions calculated for SS & DS pairs independently

How does the imbalance in N SS and N DS pairs affect C_{llr} ?

Which system is best?



- 2 systems (20 SS/180 DS)
- differing only in % false hits/ misses

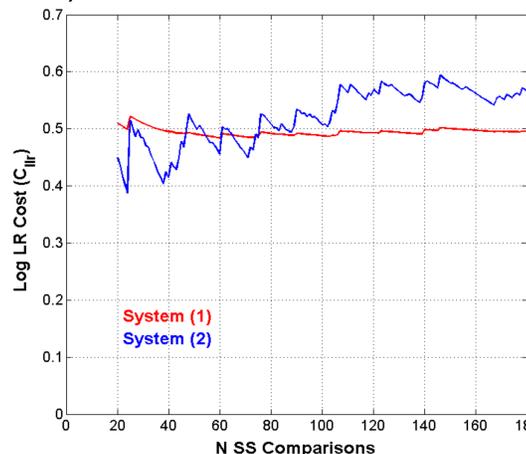
	(1)	(2)
EER	10%	10%
C_{llr}	0.50	0.44

- C_{llr} lower for system with higher % misses

3. Experiments

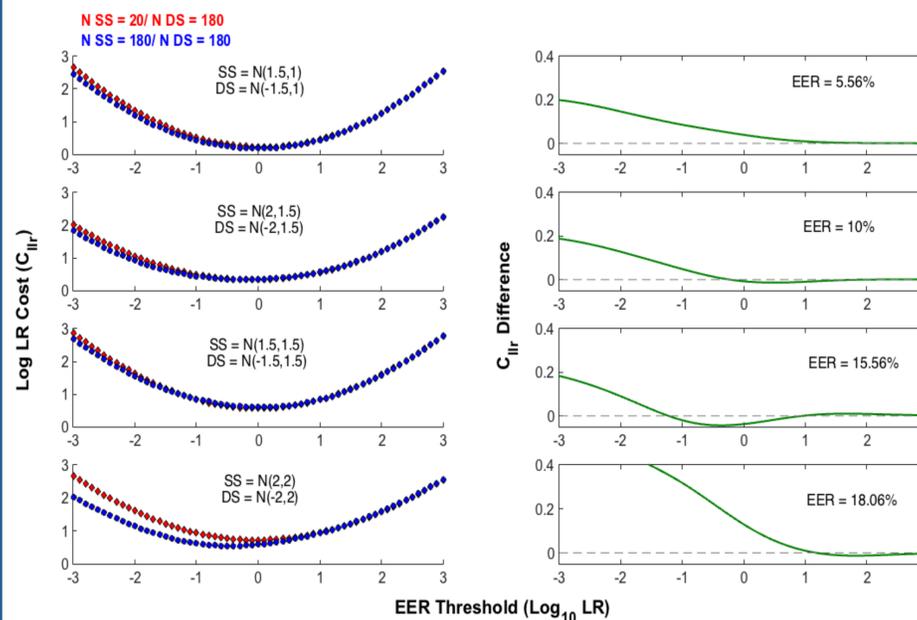
3.1 Experiment 1: what if N SS == N DS?

- hypothetical LLRs from normal distributions: SS = $N(2, 1.5)$ & DS = $N(-2, 1.5)$
- **system (1): LLR+1**
 - N SS (20:180) == N DS (20:180)
- **system (2): LLR-1**
 - N SS (20:180) \neq N DS (180)
- C_{llr} calculated as N SS increased from 20 to 180



3.2 Experiment 2: how does the threshold for EER affect C_{llr} when N SS and N DS are (im)balanced?

- hypothetical LLRs from normal distributions with four EERs (5.56%, 10%, 15.56%, 18.06%)
- from each EER condition, two systems created:
 - N SS (180) == N DS (180)
 - N SS (20) \neq N DS (180)
- C_{llr} calculated as EER threshold shifted from -3 to +3



4. Discussion

- systems with higher % misses generate better C_{llr} than systems with higher % false hits
 - N SS LLRs < N DS LLRs \therefore cost is lower

Experiment 1:

- smaller N SS (as is the case in system testing) generates better C_{llr} than if N SS == N DS
- absolute N pairs doesn't affect C_{llr} if N SS == N DS (as long as there are a sufficient number of comparisons to calculate validity in the first place)

Experiment 2:

- as in Exp 1, systems with imbalanced N SS and N DS generate better C_{llr}
- magnitude of C_{llr} differences between balanced and imbalanced systems dependent on:
 - **EER:** systems with higher EER will show a greater effect for SS/DS imbalance)
 - **LLR value at the EER:** the further the EER threshold from 0 (towards negative values), the greater the effect of SS/DS imbalance

What use is validity anyway?

- validity = means of comparing multiple systems (e.g. different input variables, modelling techniques...)
- **but** the absolute validity of the system used in a case is not of use to the trier-of-fact (in fact, it may be misleading)
 - **validity is a property of the system rather than the LR for a single comparison**
 - more useful for the court to have a credible interval (CI) or the LR of the LR

5. Conclusion

- when comparing systems it is worth considering the performance when N SS == DS, rather than just the absolute C_{llr}